

ABSTRACT. We show that Connes' embedding problem for  $\text{II}_1$ -factors is equivalent to a statement about distributions of sums of self-adjoint operators with matrix coefficients. This is an application of a linearization result for finite von Neumann algebras, which is proved using asymptotic second-order freeness of Gaussian random matrices.