

ABSTRACT. Let X be a smooth projective curve. Here we give conditions on r, d, v (essentially, existence of special spanned line bundles on X with many sections) for the existence of a rank r spanned vector bundle E on X with $\text{rank}(E) = r$, $\text{deg}(E) = d$ and $h^0(X, E) \geq v$.