

ABSTRACT. In this paper we investigate three unsolved conjectures in geometric combinatorics, namely Falconer's distance set conjecture, the dimension of Furstenburg sets, and Erdős's ring conjecture. We formulate natural  $\delta$ -discretized versions of these conjectures and show that in a certain sense that these discretized versions are equivalent.