ABSTRACT. Let P be a non-positively curved polygon of finite groups. The group P acts on a contractible 2-complex  $X_P$ , and we prove that this complex is a building if and only if the links have (angular) diameter  $\pi$ . When P has zero group theoretic curvature, a geometric argument shows that the periodic apartments are dense in the set of all apartments.